

# Optimization of Static Problem (Static Design) By Taguchi Method (Taguchi Design) Using Minitab

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## Abstract

A process to be optimized has several control factors which directly decide the target or desired value of the output. The optimization then involves determining the best control factor levels so that the output is at the target value. Such a problem is called as a "STATIC PROBLEM".

**Key words:** static design , Taguchi design ,S/N ratio, SMALLER-THE-BETTER, LARGER-THE-BETTER, NOMINAL-THE-BEST

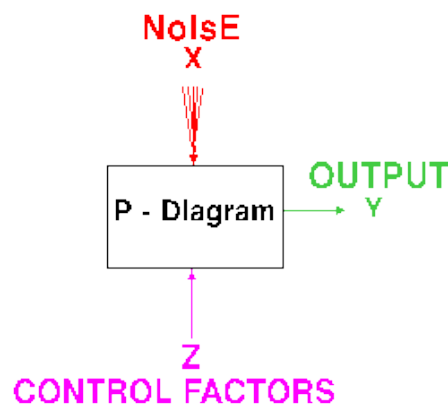
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## I. Introduction



### P - Diagram for STATIC problems

This is best explained using a P-Diagram which is shown below ("P" stands for Process or Product). Noise is shown to be present in the process but should have no effect on the output! This is the primary aim of the Taguchi experiments - to minimize variations in output even though noise is present in the process. The process is then said to have become ROBUST.

The method is applicable over a wide range of engineering fields that include processes that manufacture raw materials, sub systems, products for professional and consumer markets. In fact, the method can be applied to any process be it engineering fabrication, computer-aided-design, banking and service sectors etc. Taguchi method is useful for 'tuning' a given process for 'best' results.

**STATIC PROBLEM (BATCH PROCESS OPTIMIZATION) :**

**There are 3 Signal-to-Noise ratios of common interest for optimization of Static Problems;**

- **SMALLER-THE-BETTER :**  
 $n = -10 \text{ Log}_{10} [ \text{mean of sum of squares of measured data} ]$

This is usually the chosen S/N ratio for all undesirable characteristics like " defects " etc. for which the ideal value is zero. Also, when an ideal value is finite and its maximum or minimum value is defined (like maximum purity is 100% or maximum Temperature is 92K or minimum time for making a telephone

connection is 1 sec) then the difference between measured data and ideal value is expected to be as small as possible. The generic form of S/N ratio then becomes,

$$n = -10 \text{Log}_{10} [ \text{mean of sum of squares of } \{ \text{measured} - \text{ideal} \} ]$$

- **LARGER-THE-BETTER :**

$$n = -10 \text{Log}_{10} [ \text{mean of sum squares of reciprocal of measured data} ]$$

This case has been converted to SMALLER-THE-BETTER by taking the reciprocals of measured data and then taking the S/N ratio as in the smaller-the-better case.

- **NOMINAL-THE-BEST :**

$$n = 10 \text{Log}_{10} \frac{\text{square of mean}}{\text{variance}}$$

This case arises when a specified value is MOST desired, meaning that neither a smaller nor a larger value is desirable.

Examples are;

(i) most parts in mechanical fittings have dimensions which are nominal-the-best type.

(ii) Ratios of chemicals or mixtures are nominally the best type.

e.g. Aqua 1:3 of HNO<sub>3</sub>:HCL

Ratio of Sulphur, KNO<sub>3</sub> and Carbon in gun powder

(iii) Thickness should be uniform in deposition /growth /plating /etching..

**ANALYSIS OF STATIC PROBLEM (static design)**

In this static problem I also used same problem as previous used . only for better result and graph .

An engineer for a golf equipment manufacturer wants to design a new golf ball that has better flight distance. The engineer has identified four control factors (core material, core diameter, number of dimples, and cover thickness) and one noise factor (type of golf club). Each control factor has 2 levels. Because there is no signal factor, the engineer creates a static Taguchi design.

Minitab displays a summary of the L8 design, which includes 4 factors and 8 runs.

The Minitab worksheet shows the settings for each factor for all 8 experimental runs.

**Taguchi Design**

Design Summary

Taguchi Array L8(2<sup>4</sup>)

Factors: 4

Runs: 8

**Columns of L8(2<sup>7</sup>) array: 1 2 4 7**

	<b>C1</b>	<b>C2</b>	<b>C3</b>	<b>C4</b>
	<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>
1	1	1	1	1
1	1	2	2	2
1	2	1	2	2
1	2	2	1	1
2	1	1	2	2
2	1	2	1	1
2	2	1	1	1
2	2	2	2	2

**II. Results**

An engineer for a golf equipment manufacturer wants to design a new golf ball to maximize ball flight distance. The engineer has identified four control factors (core material, core diameter, number of dimples, and cover thickness) and one noise factor (type of golf club). Each control factor has 2 levels. The noise factor is two types of golf clubs: driver and a 5-iron. The engineer measures flight distance for each club type, and records the data in two noise factor columns in the worksheet.

Because the goal of the experiment is to maximize flight distance, the engineer uses the larger-is-better signal-to-noise ratio (S/N). The engineer also wants to test the interaction between core material and core diameter.

In Taguchi experiments, you always want to maximize the S/N ratio. In this example, the ranks indicate that core diameter (B) has the most influence on both the S/N ratio and the mean. For S/N ratio, cover thickness (D) has the next largest influence, followed by core material (A) and dimples (C). For means, core material (A) has the next largest influence, followed by dimples (C) and cover thickness (D).

For this problem, because the goal is to increase ball flight distance, the engineer wants the factor levels that produce the highest mean. The levels averages in the response tables show that the S/N ratios and the means are maximized at the Level 1 value for each factor, which corresponds with the following factor settings.

- Liquid core (A)
- Core diameter (B) = 118
- Dimples (C) = 392
- Cover thickness (D) = 0.06
- The main effects plots and the interaction plots confirm these results. The interaction plots show that, with the liquid core, the flight distance is maximized when the core diameter is 118.
- To continue this analysis, the engineer can use Predict Taguchi Results to determine the predicted S/N ratios and means at these factor settings

Linear Model Analysis: SN ratios versus Material, Diameter, Dimples, Thickness

Estimated Model Coefficients for SN ratios

Term	Coef	SE Coef	T	P
Constant	38.181	0.4523	84.418	0.000
Material Liquid	3.436	0.4523	7.596	0.017
Diameter 118	3.967	0.4523	8.772	0.013
Dimples 392	2.982	0.4523	6.593	0.022
Thicknes 0.03	-3.479	0.4523	-7.692	0.016
Material*Diameter Liquid 118	1.640	0.4523	3.625	0.068

Model Summary

S	R-Sq	R-Sq(adj)
1.2793	99.21%	97.23%

Analysis of Variance for SN ratios

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Material	1	94.427	94.427	94.427	57.70	0.017
Diameter	1	125.917	125.917	125.917	76.94	0.013
Dimples	1	71.133	71.133	71.133	43.47	0.022
Thickness	1	96.828	96.828	96.828	59.17	0.016
Material*Diameter	1	21.504	21.504	21.504	13.14	0.068
Residual Error	2	3.273	3.273	1.637		
Total	7	413.083				

Linear Model Analysis: Means versus Material, Diameter, Dimples, Thickness

Estimated Model Coefficients for Means

Term	Coef	SE Coef	T	P
Constant	110.40	8.098	13.634	0.005
Material Liquid	36.86	8.098	4.552	0.045
Diameter 118	51.30	8.098	6.335	0.024
Dimples 392	23.25	8.098	2.871	0.103
Thicknes 0.03	-22.84	8.098	-2.820	0.106
Material*Diameter Liquid 118	31.61	8.098	3.904	0.060

Model Summary

S	R-Sq	R-Sq(adj)
22.9035	97.88%	92.58%

Analysis of Variance for Means

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Material	1	10871	10871	10870.8	20.72	0.045
Diameter	1	21054	21054	21053.5	40.13	0.024
Dimples	1	4325	4325	4324.5	8.24	0.103
Thickness	1	4172	4172	4172.4	7.95	0.106
Material*Diameter	1	7995	7995	7994.8	15.24	0.060
Residual Error	2	1049	1049	524.6		
Total	7	49465				

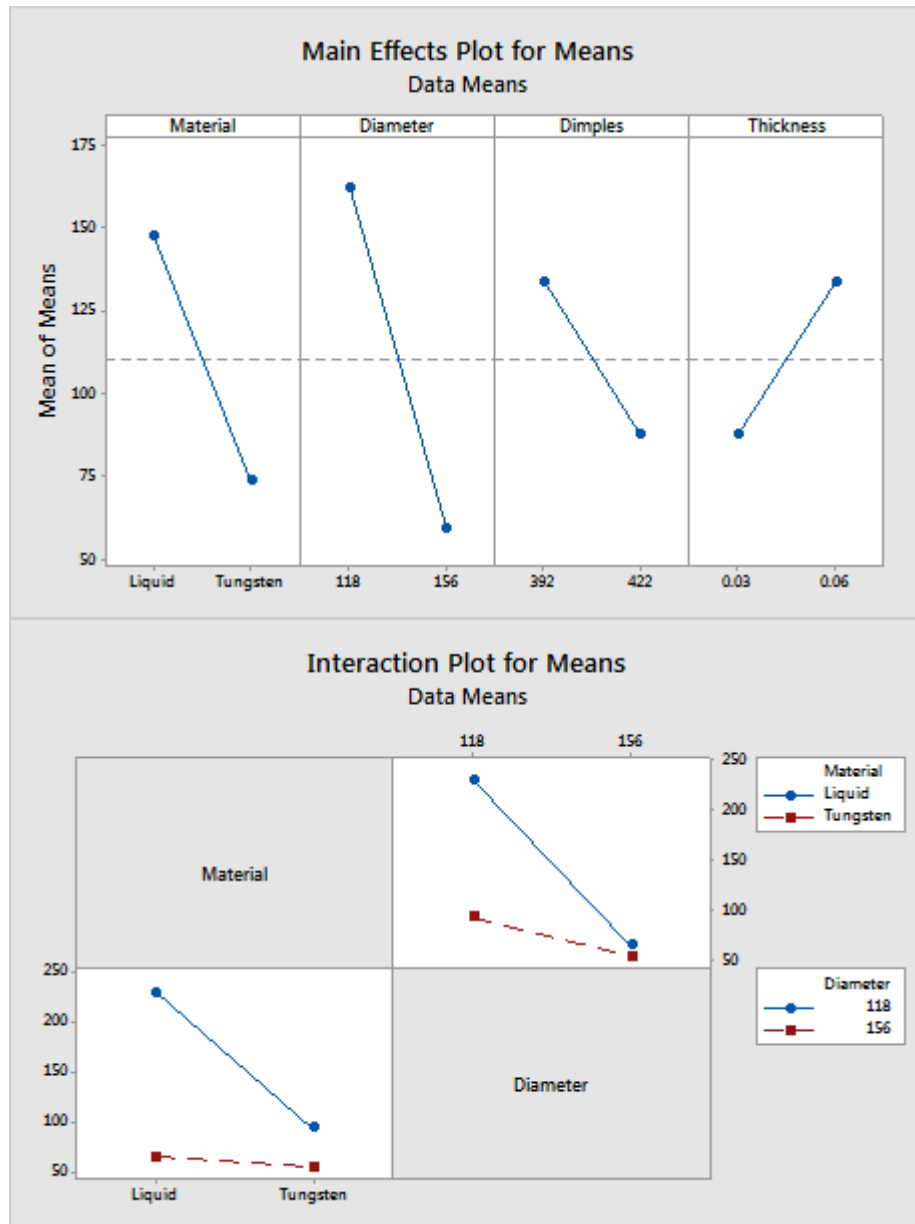
Response Table for Signal to Noise Ratios

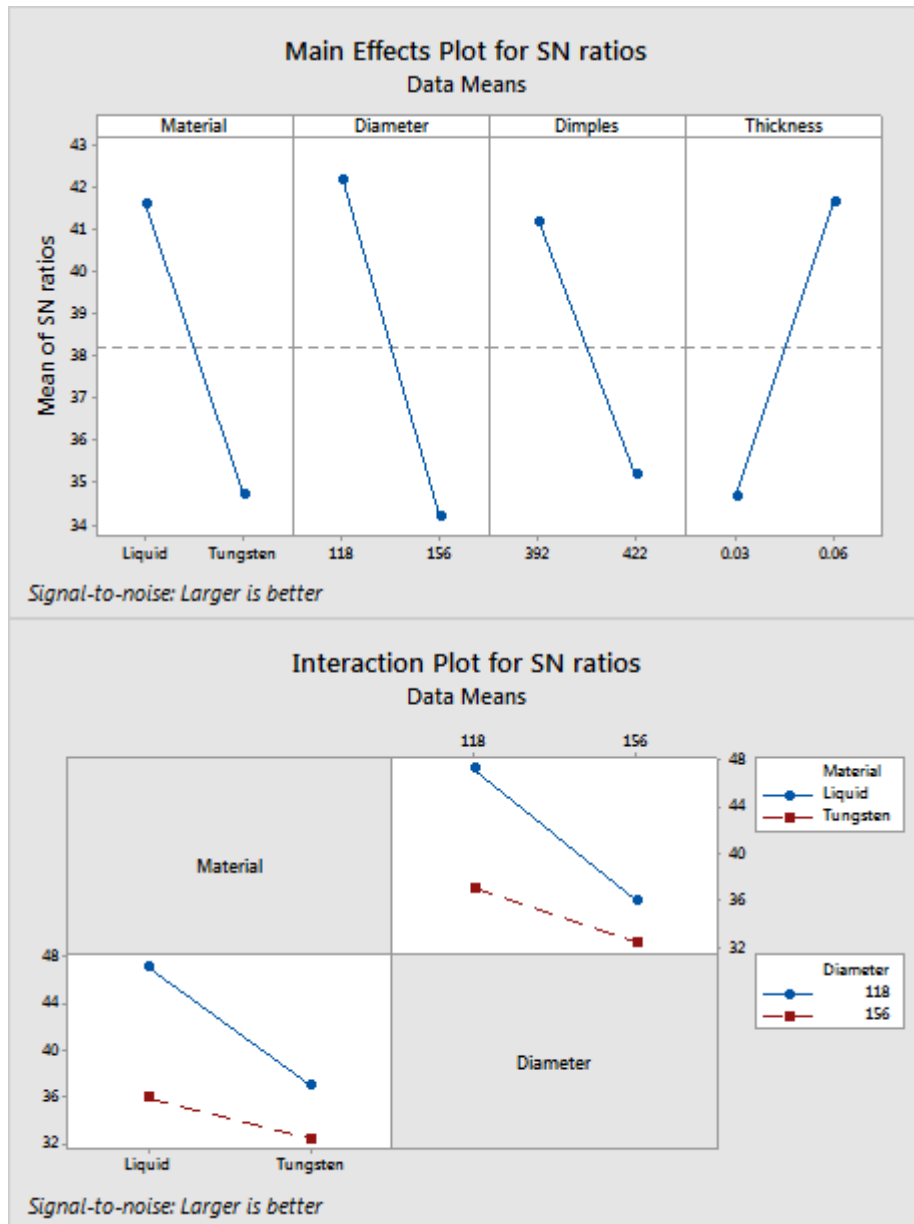
Larger is better

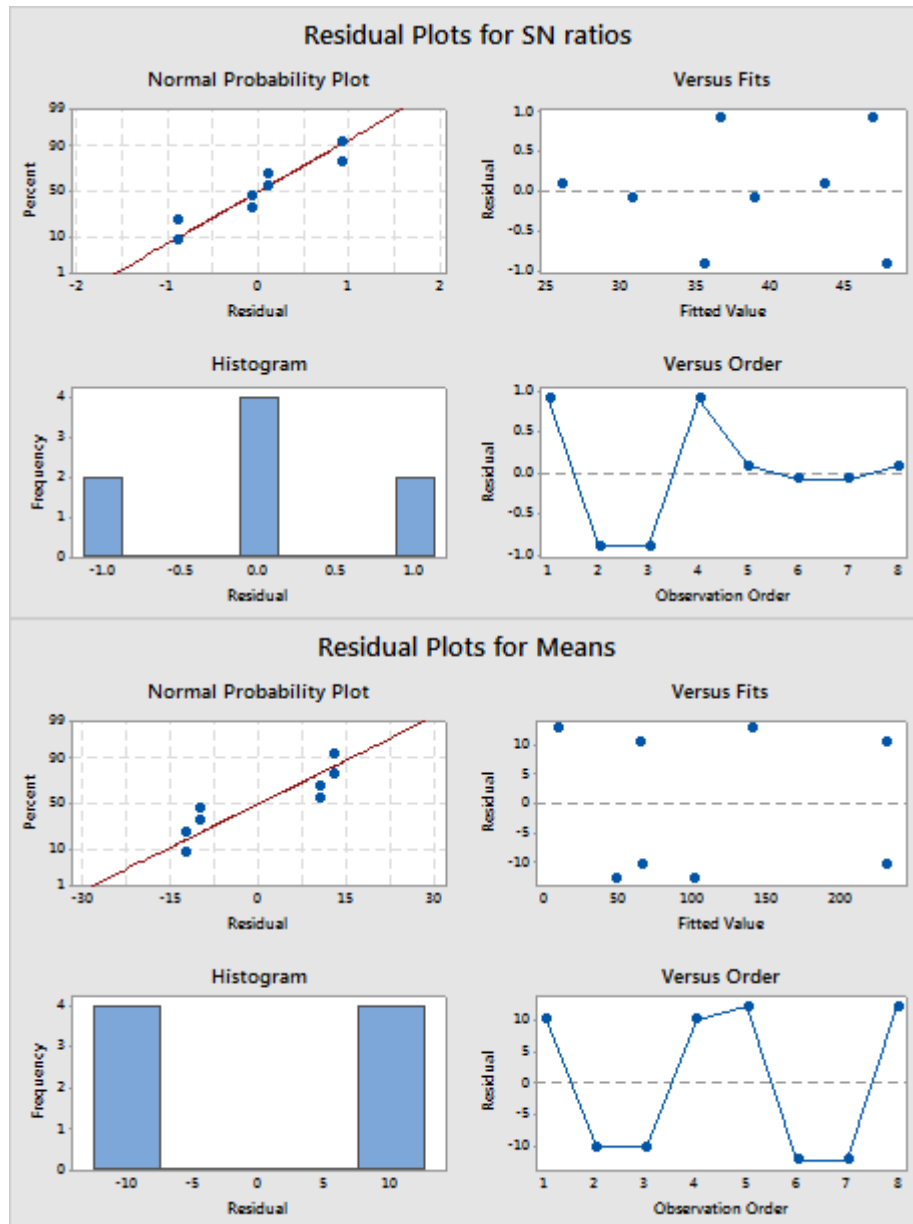
Level	Material	Diameter	Dimples	Thickness
1	41.62	42.15	41.16	34.70
2	34.75	34.21	35.20	41.66
Delta	6.87	7.93	5.96	6.96
Rank	3	1	4	2

Response Table for Means

Level	Material	Diameter	Dimples	Thickness
1	147.26	161.70	133.65	87.56
2	73.54	59.10	87.15	133.24
Delta	73.73	102.60	46.50	45.68
Rank	2	1	3	4







### III. CONCLUSION

- In the above discussion, for S/N ratios, all the factors have a p-value less than 0.05 and are statistically significant at a significance level of 0.05. Frequently, a significance level of 0.10 is used for evaluating terms in a model.
- The interaction is statistically significant at a significance level of 0.10. For means, core material ( $p = 0.045$ ) and core diameter ( $p = 0.024$ ) are statistically significant at a significance level of 0.05, and the interaction of material with diameter ( $p = 0.06$ ) is statistically significant at a significance level of 0.10.
- Minitab prominently provides an estimated regression coefficients table for each response characteristic that you select. In this above problem, the engineer chose two response characteristics — the signal-to-noise ratio (S/N) and the means. Use the p-values to determine which factors are statistically significant and use the coefficients to determine each factor's relative importance in the model.

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