# A New Subclass of Classes of P-Valent Starlike and **Convex Functions with Coefficient Bounds**

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ABSTRACT: We will describe as ubclass of p-valent analytic functions in this paper and will obtain sharp upper bounds of the functional  $|a_{p+2}-\mathbb{Z}a_{p+1}^2|$  for the analytic function  $f(z)=z^p+\sum_{n=p+1}^\infty a_n\,z^n$ , |z|<1belonging to this subclass.

KEYWORDS: Univalent functions, Starlike functions, Close to convex functions and bounded functions.

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#### **Introduction:**

Let  $\mathcal{A}$  denote the class of functions of the form

$$f(z) = z + \sum_{n=2}^{\infty} a_n z^n$$
 (1.1)

which are analytic in the unit disc  $\mathbb{E} = \{z: |z| < 1\}$ . Let **S** be the class of functions of the form (1.1), which are analytic univalent in E.

In 1916, Bieber Bach ([7], [8]) proved that  $|a_2| \le 2$  for the functions  $f(z) \in S$ . In 1923, Löwner [5] proved that  $|a_3| \leq 3$  for the functions  $f(z) \in S$ ..

With the known estimates  $|a_2| \le 2$  and  $|a_3| \le 3$ , it was natural to seek some relation between  $a_3$  and  $a_2^2$ for the class S, Fekete and Szegö[9] used Löwner's method to prove the following well known result for the class S.

Let 
$$f(z) \in \mathcal{S}$$
, then
$$3 - 4\mathbb{Z}, if \mathbb{Z} \le 0;$$

$$|a_3 - \mathbb{Z}a_2^2| \le \begin{bmatrix} 3 - 4\mathbb{Z}, if \ \mathbb{Z} \le 0; \\ 1 + 2\exp\left(\frac{-2\mathbb{Z}}{1 - \mathbb{Z}}\right), if \ 0 \le \mathbb{Z} \le 1; (1.2) \\ 4\mathbb{Z} - 3, if \mathbb{Z} \ge 1. \end{bmatrix}$$

The inequality (1.2) plays a very important role in determining estimates of higher coefficients for some sub classes **S** (See Chhichra[1], Babalola[6]).

Let us define some subclasses of S.

We denote by S\*, the class of univalent starlike functions

$$g(z) = z + \sum_{n=2}^{\infty} b_n z^n \in \mathcal{A}$$
 and satisfying the condition  $Re\left(\frac{zg(z)}{g(z)}\right) > 0, z \in \mathbb{E}.$  (1.3)

We denote by  $\mathcal{K}$ , the class of univalent

$$Re\left(\frac{zg(z)}{g(z)}\right) > 0, z \in \mathbb{E}.$$
 (1.3)

convex functions

$$h(z) = z + \sum_{n=2}^{\infty} c_n z^n$$
,  $z \in \mathcal{A}$  and satisfying the condition
$$R_{\mathcal{A}} \frac{((zh'(z)))}{(zh'(z))} > 0, z \in \mathbb{F}(1.4)$$

$$Re^{\frac{\left(\left(zh^{'}(z)\right)}{h^{'}(z)}} > 0, z \in \mathbb{E}.(1.4)$$

#### p-VALENT FUNCTION:

Multivalent functions and in particular p-valent functions, are a generalization of univalent functions. In the study of univalent functions, one of the fundamental problems is whether there exists a univalent mapping from a given domain E onto a given domain D. A necessary condition for the existence of such a mapping is that E and D have equal degrees of connectivity. If E and D are simply-connected domains whose boundaries contain more than one point, then this condition is also sufficient and the problem reduces to mapping a given

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domain onto a disc. In this connection, a special role is played in the theory of univalent functions on simply-connected domains by the S, class of functions f that are regular and univalent on the unit disc  $E = \{z: |z| < 1\}$ , normalized by the conditions f(0) = 0, f'(0) = 1, and having the expansion

$$f(z) = z + a_2 z^2 + a_3 z^3 + - - -, z \in E$$

In the case of multiply-connected domains, mappings of a given multiply-connected domain onto so-called canonical domains are studied. In particular, p-valent functions can be defined as follow:

Let  $\mathcal{A}_{\mathbf{n}}(\mathbf{p})$  is a positive integer)denote the class of functions of the form

$$f(z) = z^p + \sum_{k=1}^{\infty} a_{p+k} z^{p+k}$$

which are analytic in the unit disc E. Clearly,  $\mathcal{A}_1 = \mathcal{A}$ . A function  $f(z) \in \mathcal{A}_p$  is said to be p-valent in E if it assumes no value more than p times in E.

## p-VALENT STARLIKE FUNCTION:

A function  $f(z) \in \mathcal{A}_p$  is said to be a p-valent starlike function in E if there exists a positive real number  $\rho$  such that

$$Re\left(\frac{zf'(z)}{f(z)}\right) > 0$$
and
$$\int_{0}^{\pi} \left[ Re\left(\frac{zf'(z)}{f(z)}\right) \right] d\theta = 2p\pi, z = re^{i\theta} for$$

$$\rho < |z| < 1.$$

We denote the class of p-valent starlike functions by  $S_p^*$ . By  $S_p^*(\beta)$ , we denote the class of functions  $f(z) \in \mathcal{A}_p$  satisfying the condition

$$Re\left(\frac{zf^{'}(z)}{f(z)}\right) > \beta; 0 \le \beta < p, z \in E$$

Note: p-valent starlike functions are also called p-valently starlike functions.

 $f(z) \in S_p^*(\beta)$  is called p-valently starlike function of order  $\beta$ .

We introduce a new subclassas  $\left\{ \mathbf{f}(\mathbf{z}) \in \mathcal{A}_{\mathbf{p}}; \frac{\left[\mathbf{z}\left\{\mathbf{z}\mathbf{f}'(\mathbf{z})\right\}'\right]'}{\mathbf{p}\left\{\mathbf{z}\mathbf{f}'(\mathbf{z})\right\}'} < \frac{\mathbf{1}+\mathbf{Az}}{\mathbf{1}+\mathbf{Bz}}; \mathbf{z} \in \mathbb{E} \right\}$  and we will denote this class as  $f(z) \in \mathcal{H}_{n}^{*}$ .

Symbol ≺ stands for subordination, which we define as follows:

**Principle of Subordination:** Let f(z) and F(z) be two functions analytic in  $\mathbb{E}$ . Then f(z) is called subordinate to F(z) in  $\mathbb{E}$  if there exists a function w(z) analytic in  $\mathbb{E}$  satisfying the conditions w(0) = 0 and |w(z)| < 1 such that f(z) = F(w(z));  $z \in \mathbb{E}$  and we write f(z) < F(z).

By  $\mathcal{U}$ , we denote the class of analytic bounded functions of the form  $w(z) = \sum_{n=1}^{\infty} d_n z^n$ , w(0) = 0, |w(z)| < 1. (1.5)

It is known that  $|d_1| \le 1$ ,  $|d_2| \le 1 - |d_1|^2$ . (1.6)

## II. PRELIMINARY LEMMAS:

For 
$$0 < c < 1$$
, we write  $w(z) = \left(\frac{c+z}{1+cz}\right)$  so that 
$$\frac{\frac{1+w(z)}{1-w(z)}}{1-w(z)} = 1 + 2c_1z + 2(c_2+c_1^2)z^2 + - - -(2.1)$$
 Here  $|c_1| \le 1$ ,  $|c_2| \le 1$ -  $|c_1|^2$  (2.2)

#### III. MAIN RESULTS

**THEOREM 3.1**: Let  $f(z) \in \mathcal{H}_{p}^{*}$ , then

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$$\left|a_{p+2} - \mu a_{p+1}^{2}\right| \leq \begin{cases} \frac{(A-B)p^{3}[(A-B)p-B]}{2(p+2)^{2}} - \mu \frac{(A-B)^{2}p^{6}}{(p+1)^{4}} \\ if \ \mu \leq \frac{[(A-B)p-(B+1)](p+1)^{4}}{2(p+2)^{2}(A-B)p^{3}} & (3.1) \\ \frac{(A-B)p^{3}}{2(p+2)^{2}} \\ if \frac{[(A-B)p-(B+1)](p+1)^{4}}{2(p+2)^{2}(A-B)p^{3}} \leq \mu \leq \frac{[1-B+(A-B)p](p+1)^{4}}{2(p+2)^{2}(A-B)p^{3}} & (3.2) \\ \mu \frac{(A-B)^{2}p^{6}}{(p+1)^{4}} - \frac{(A-B)p^{3}[(A-B)p-B]}{2(p+2)^{2}} \\ if \ \mu \geq \frac{[1-B+(A-B)p](p+1)^{4}}{2(p+2)^{2}(A-B)p^{3}} & (3.3) \end{cases}$$

The results are sharp.

**Proof:** By definition of  $f(z) \in \mathcal{H}_n^*$ , we have

$$\frac{\left[\mathbf{z}\left\{\mathbf{z}\mathbf{f}'\left(\mathbf{z}\right)\right\}'\right]'}{\mathbf{p}\left\{\mathbf{z}\mathbf{f}'\left(\mathbf{z}\right)\right\}'} = \frac{1+Az}{1+Bz}; w(z) \in \mathcal{U}.(3.4)$$

Expanding the series (3.4), we get

$$p^{3}z^{p-1} + a_{p+1}(p+1)^{3}z^{p} + a_{p+2}(p+2)^{3}z^{p+1} + --- = (1 + c_{1}(A-B)z + (A-B)(c_{2} - Bc_{1}^{2})z^{2} + ---)(p^{3}z^{p-1} + pa_{p+1}(p+1)^{2}z^{p} + pa_{p+2}(p+2)^{2}z^{p+1} + ---) (3.5)$$

Identifying terms in (3.5), we get

Identifying terms in (3.5), we get
$$a_{p+1} = \frac{c_1(A-B)p^3}{(p+1)^2}(3.6)$$

$$a_{p+2} = \frac{c_1^2(A-B)^2p^4 + (A-B)(c_2 - Bc_1^2)p^3}{2(p+2)^2}(3.7)$$
From (3.6) and (3.7), we obtain

From (3.6) and (3.7), we obtain

$$a_{p+2-}\mu a_{p+1}^2 = \frac{c_1^2 (A-B)^2 p^4 + (A-B)(c_2 - Bc_1^2) p^3}{2(p+2)^2} - \mu \frac{c_1^2 (A-B)^2 p^6}{(p+1)^4} (3.8)$$

Taking absolute value, (3.8) can be rewritten as 
$$|a_{p+2} - \mu a_{p+1}^2| \le \frac{|c_2|(A-B)p^3}{2(p+2)^2} + \left| \frac{(A-B)^2 p^4 - B(A-B)p^3}{2(p+2)^2} - \mu \frac{(A-B)^2 p^6}{(p+1)^4} \right| |c_1|^2 (3.9)$$

Using (2.2) in (3.9), we get 
$$|a_{p+2} - \mu a_{p+1}^2| \leq \frac{2(p+2)^2}{2(p+2)^2} + \left| \frac{2(p+2)^2}{2(p+2)^2} + \frac{(p+1)^4}{(p+1)^4} \right|^{4} |c_1|^2 (3.10)$$

$$\underline{\mathbf{Case I:}} \mu \leq \frac{[(A-B)p-B](p+1)^4}{2(p+2)^2(A-B)p^3}$$
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Case I:
$$\mu \le \frac{[(A-B)p-B](p+1)^4}{2(p+2)^2(A-B)p^3}$$

(3.10) can be rewritten as

$$|a_{p+2} - \mu a_{p+1}^2| \le \frac{(1 - |c_1|^2)(A - B)p^3}{2(p+2)^2} + \left(\frac{(A - B)^2 p^4 - B(A - B)p^3}{2(p+2)^2} - \mu \frac{(A - B)^2 p^6}{(p+1)^4}\right) |c_1|^2$$

$$|a_{p+2} - \mu a_{p+1}^2| \le \frac{(A - B)p^3}{2(p+2)^2} + \left(\frac{(A - B)^2 p^4 - (B + 1)(A - B)p^3}{2(p+2)^2} - \mu \frac{(A - B)^2 p^6}{(p+1)^4}\right) |c_1|^2 (3.11)$$
Subcase I (a):  $\mu \le \frac{[(A - B)p - (B + 1)](p+1)^4}{2(p+2)^2(A - B)p^3}$ 

Subcase I (a): 
$$\mu \leq \frac{[(A-B)p-(B+1)](p+1)^4}{2(p+2)^2(A-B)p^3}$$

Using (2.2), (3.11) becomes

$$|a_{p+2} - \mu a_{p+1}^2| \le \frac{(A-B)p^3[(A-B)p-B]}{2(p+2)^2} - \mu \frac{(A-B)^2p^6}{(p+1)^4}$$
(3.12)

Using (2.2), (3.11) becomes
$$|a_{p+2} - \mu a_{p+1}^2| \le \frac{(A-B)p^3[(A-B)p-B]}{2(p+2)^2} - \mu \frac{(A-B)^2p^6}{(p+1)^4} (3.12)$$
**Subcase I (b)**:  $\mu \ge \frac{[(A-B)p-(B+1)](p+1)^4}{2(p+2)^2(A-B)p^3}$ . We obtain from (3.11)
$$|a_{p+2} - \mu a_{p+1}^2| \le \frac{(A-B)p^3}{2(p+2)^2} (3.13)$$

$$|a_{p+2} - \mu a_{p+1}^2| \le \frac{(A-B)p^3}{2(p+2)^2} (3.13)$$

Case II: 
$$\mu \ge \frac{[(A-B)p-B](p+1)^4}{2(p+2)^2(A-B)p^3}$$

Preceding as in case I, we get
$$\left|a_{p+2} - \mu a_{p+1}^{2}\right| \leq \frac{(A-B)p^{3}}{2(p+2)^{2}} - \left(\frac{(A-B)^{2}p^{4} + (1-B)(A-B)p^{3}}{2(p+2)^{2}} - \mu \frac{(A-B)^{2}p^{6}}{(p+1)^{4}}\right) |c_{1}|^{2}$$
Subcase II (a):  $\mu \geq \frac{[1-B+(A-B)p](p+1)^{4}}{2(p+2)^{2}(A-B)p^{3}}$ 
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(3.14) takes the form

$$|a_{p+2} - \mu a_{p+1}^2| \le |a_{p+2} - \mu a_{p+1}^2| \le \frac{(A-B)p^3}{2(p+2)^2} - \left(\frac{(A-B)^2p^4 + (1-B)(A-B)p^3}{2(p+2)^2} - \mu \frac{(A-B)^2p^6}{(p+1)^4}\right)$$

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$$|a_{p+2} - \mu a_{p+1}^2| \le \mu \frac{(A-B)^2 p^6}{(p+1)^4} - \frac{(A-B)p^3 [(A-B)p - B]}{2(p+2)^2}$$
(3.15)

**Subcase II (b)**:  $\mu \le \frac{[1-B+(A-B)p](p+1)^4}{2(p+2)^2(A-B)p^3}$ 

Preceding as in subcase I (b), we get

$$|a_{p+2} - \mu a_{p+1}^2| \le \frac{(A-B)p^3}{2(p+2)^2} \tag{3.16}$$

Combining (3.12), (3.13), (3.15) and (3.16), the theorem is proved

Extremal function for (3.1) and (3.3) is defined by

 $f_1(z) = (1 + az)^h$  where

$$a = \frac{(A-B)p^3(p+2)^2 - (p+1)^4((A-B)p - B)}{(p+1)^2(p+2)^2}$$

And

$$h = \frac{(A-B)p^3(p+2)^2}{(A-B)p^3(p+2)^2 - (p+1)^4((A-B)p - B)}$$

Extremal function for (3.2) is defined by

$$f_2(z) = z \left(1 + \frac{p^3 z}{2(p+2)^2}\right)^{(A-B)}$$

Corollary 3.2: Putting A = 1, B = -1 in the theorem

$$\left|a_{p+2-\mu a_{p+1}^2}\right| \le \begin{cases} \frac{p^3(2p+1)}{(p+2)^2} - \frac{4\mu p^6}{(p+1)^4} & \text{if } \mu \le \frac{(p+1)^4}{2p^2(p+2)^2} \\ \frac{p^3}{(p+2)^2} & \text{if } \frac{(p+1)^4}{2p^2(p+2)^2} \le \mu \le \frac{(p+1)^5}{2p^3(p+2)^2} \\ \frac{4\mu p^6}{(p+1)^4} - \frac{p^3(2p+1)}{(p+2)^2} & \text{if } \mu \ge \frac{(p+1)^5}{2p^3(p+2)^2} \end{cases}$$

**Corollary 3.3:** Putting p = 1 in the theorem, we get

tring 
$$p = 1$$
 in the theorem, we get
$$|a_{3-}\mu a_{2}|^{2} \le \begin{cases} \frac{(A-B)(A-2B)}{18} - \mu \frac{(A-B)^{2}}{16} & \text{if } \mu \le \frac{8(A-2B-1)}{9(A-B)} \\ \frac{(A-B)}{18} & \text{if } \frac{8(A-2B-1)}{9(A-B)} \le \mu \le \frac{8(A-2B+1)}{9(A-B)} \\ \frac{\mu(A-B)^{2}}{16} - \frac{(A-B)(A-2B)}{18} & \text{if } \mu \ge \frac{8(A-2B+1)}{9(A-B)} \end{cases}$$

**Corollary 3.4:** Putting A = 1, B = -1, p = 1 in the theorem

$$|a_3 - \mu a_2^2| \le \begin{cases} \frac{1}{3} - \frac{\mu}{4} & \text{if } \mu \le \frac{8}{9} \\ \frac{1}{9} & \text{if } \frac{8}{9} \le \mu \le \frac{16}{9} \\ -\frac{1}{3} + \frac{\mu}{4} & \text{if } \mu \ge \frac{16}{9} \end{cases}$$

These estimates were derived by Keogh and Merkes [8] and are results for the class of univalent convex functions.

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## A New Subclassof Classes Of P-Valent Starlike And Convex Functions With Coefficient Bounds

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