

A Study on Performance Analysis of Different Prediction Techniques in Prediction of Time Series Data

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ABSTRACT: Time series data is a series of statistical data that is related to a specific instant or a specific time period. Here, the measurements are recorded on a regular basis such as monthly, quarterly and yearly. Most of the researchers have used one of the prediction techniques in prediction of time series data. But, they have not tested all prediction techniques on same data set. They have not even compared the performance of different prediction techniques on the same data set. In this research work, some well known prediction techniques have been applied in the same time series data set. The average error and residual analysis have been done for each and every applied technique. One technique has been selected based on the minimum average error and residual analysis among the all applied techniques. The residual analysis comprises of absolute residual, maximum residual, median of absolute residual, mean of absolute residual and standard deviation. To finalize the algorithm, same procedure has been applied on different time series data sets. Finally, one technique has been selected which has been given minimum error and minimum value of residual analysis in most cases.

Keywords: Time Series Data, Linear Trend Equation, Logarithmic Trend Equation, Simple Moving Average, Exponential Moving Average, Single Exponential Smoothing, Double Exponential Smoothing, ANN, Residual Analysis.

I. INTRODUCTION

A time series is a sequence of data points, measured typically at successive times spaced at uniform time intervals. Examples of time series are the daily closing value of the Dow Jones index or the annual flow volume of the Nile River at Aswan, weather data, climate data, Cepheid variables stars, Ecological fluctuations. Time series are very frequently plotted via line charts. Time series data have a natural temporal ordering. This makes time series analysis distinct from other common data analysis problems, in which there is no natural ordering of the observations (e.g. explaining people's wages by reference to their education level, where the individuals' data could be entered in any order). Time series analysis is also distinct from spatial data analysis where the observations typically relate to geographical locations (e.g. accounting for house prices by the location as well as the intrinsic characteristics of the houses).

Time Series Data Prediction is applied on Prediction, Noise Reduction, Scientific Insight, and Control.

There are several prior works done where an effort has been made to predict the Time Series Data but the performance of different methods applied on same database has not been measured. Here in this paper an effort has been made to analyze the performance of different prediction technique.

II. PROPOSED WORK

Our proposed work consists of performance analysis of different statistical methods for time series prediction, they are linear trend, logarithmic trend, simple moving average, exponential moving average, different smoothing algorithms, and they are single exponential smoothing, double exponential smoothing and ANN. The performance analysis is based on the result of residual analysis.

A. Statistical Methods

In these process different statistical methods for time series prediction has been used. They are

A.1 Linear Trend Equation

The long-term trend of many business series, such as sales, exports, and production, often approximates a straight line. If so, the equation to describe this growth is

$$Y' = a + bt$$

Where

Y' read Y prime, is the projected value of the Y variable for a selected value of t . a is the Y -intercept. It is the estimated value of Y when $t=0$. b is the slope of the line, or the average change in Y' for each change of one unit in t . it is any value of time that is selected.

A.2 Logarithmic Trend Equation:

The trend equation for a time series that does approximate a curvilinear trend may be computed by using the logarithms of the data and the least squares method.

$$\log Y' = \log a + \log b (t)$$

Where

Y' read Y prime, is the projected value of the Y variable for a selected value of t.

a is the Y-intercept. It is the estimated value of Y when t0.

b is the slope of the line, or the average change in Y' for each change of one unit in t.

A.3 Simple Moving Average

In financial applications a simple moving average (SMA) is the unweighted mean of the previous n data. However, in science and engineering the mean is normally taken from an equal number of data on either side of a central value. This ensures that variations in the mean are aligned with the variations in the data rather than being shifted in time. An example of a simple equally weighted running mean for a n-day sample of closing price is the mean of the previous n days' closing prices.

those prices are $p_M, p_{M-1}, \dots, p_{M-(n-1)}$ then the formula is

$$SMA = \frac{p_M + p_{M-1} + \dots + p_{M-(n-1)}}{n}$$

A.4 Exponential Moving Average

An exponential moving average (EMA), also known as an exponentially weighted moving average (EWMA), is a type of infinite impulse response filter that applies weighting factors which decrease exponentially. The weighting for each older datum decreases exponentially, and never reaching zero. Here we have used 5 year moving average model.

The EMA for a series Y may be calculated recursively:

$$S_1 = Y_1$$

$$\text{for } t > 1, S_t = \alpha \cdot Y_{t-1} + (1 - \alpha) \cdot S_{t-1}$$

B. Single Exponential Smoothing

It tracks the forecast performance and automatically adjust α to allow for shifting patterns.

The formula takes the form:

$$F_{t+1} = \alpha D_t + (1 - \alpha) F_t$$

Where

D_t is the original value

F_t is the forecasted value

α is the weighting factor, which ranges from 0 to 1.

t is the current time period.

C. Double Exponential Smoothing

When there is a particular trend in a time series data Single Exponential smoothing is not effective . Here Double Exponential Smoothing is used. It is similar to Single Exponential Smoothing but there is a component to pick the trend.

$$F_t = a * A_{t-1} + (1 - a) * (F_{t-1} + T_{t-1})$$

$$T_t = b * (A_{t-1} - F_{t-1}) + (1 - b) * T_{t-1}$$

$$AF_t = F_t + T_t$$

Where,

a is the Y-intercept.

b is the slope of the line

F_t = Unadjusted forecast (before trend)

T_t = Estimated trend

AF_t = Trend-adjusted forecast

D. Artificial Neural Network

Artificial neural networks are computational model inspired by human brain. It is mainly used in massively parallel, distributed system, made up of simple processing units (neurons). Synaptic connection of a ANN are strengths among neurons used to store the acquired knowledge. Knowledge of an ANN is acquired by the network from its environment through a learning process.

basic model of artificial neural network is shown in fig 1.

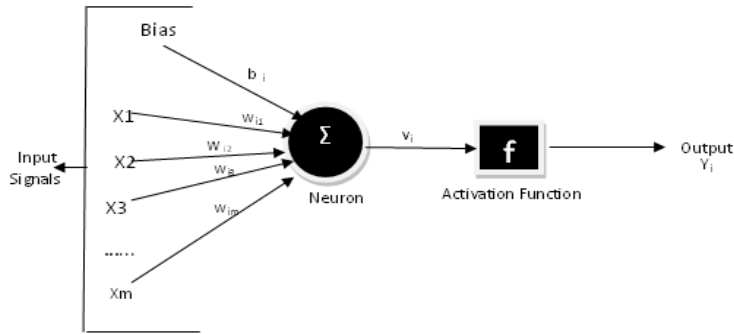


Fig 1: Model of an Artificial Neuron

Here we have used LMS Learning mechanism and used 75% data for training and 25% data for testing.

E. Residual Analysis

Absolute Residual = | (Estimated Value – Actual Value) |

Maximum Residual = Maximum(Absolute Residual)

Mean Absolute Residual = | (Estimated Value – Actual Value) | / Actual Value

Mean of Mean Absolute Residual = (Mean of Absolute Residual) / N

Median Absolute Residual = Middle Value of Absolute Residual

$$\text{Standard Deviation (SD)} = \sqrt{\frac{1}{N-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

III. EXPERIMENTAL RESULTS

These methods have been applied to different types of data sets in education sectors of India. Results are displayed in following tables.

The following table shows the database of ratio of Girls per 100 boys enrolled in middle (VI-VIII) in India 1950 to 2005-06

Data	Linear	Single exp	Log	Double exp	SMA	ANN	EMA
32	45.2579	33.43	44.84	0	0	0	0
41	47.34035	32.572	47.19	32	0	0	32
49	49.42281	37.62	49.54	57.68	48.4	49.00292	40.099
58	51.50526	44.45	51.9	69.8672	54.2	57.99736	48.11
62	53.58772	52.58	54.25	74.30988	59.2	62.00412	57.011
61	55.67017	58.23	56.58	70.6954	62.4	66.58781	61.501
66	57.75263	59.89	58.88	70.5592	63.8	65.87488	61.05
65	59.83509	63.55	61.14	67.9034	64.6	65.95779	65.595
65	61.91755	64.42	63.36	65.7959	65.8	65.76653	65.05
66	64	64.769	65.52	65.6263	67.4	65.84314	65.005
67	66.08246	65.507	67.62	66.65304	67.5	66.29375	65.9
69	68.16491	66.403	69.65	69.10862	68.2	67.37802	66.89
70	70.24737	67.961	71.6	71.01175	69.4	70.97671	68.789
69	72.32983	69.184	73.48	70.4487	71.6	73.82788	69.878
72	74.41228	69.073	75.28	72.58202	73.6	71.79055	69.0878
78	76.49474	70.829	76.99	78.98579	75.6	77.50689	71.708

Table 1: Result of Girls boys ratio in Middle (VI-VIII) Enrolled in India 1950 to 2005-06

Figure 2 graphically shows the comparison result of Girls enrollment per 100 boys in middle database.

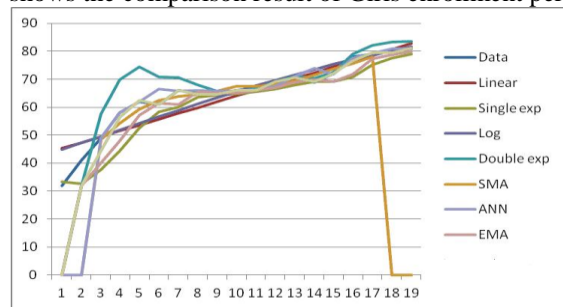


Fig 2: Comparison result of different prediction method on girls boys ratio in middle database

The following table shows the result of residual analysis of different prediction technique on girls boys ratio enrolled in India at Middle(VI-VIII) 1950 to 2005-06.

Prediction Technique	Mean of Absolute Residual	Maximum Residual	Mean of Mean of Absolute Residual	Median Absolute Residual	Standard Deviation
Linear	14	1.31	0.069	0.015	11.67
Logarithm	12.84	1.24	0.065	0.48	11.68
Single exp	13.82	1.64	0.086	2.77	13.01
Double exp	14.98	2.56	0.076	2.56	12.93
SMA	12.04	1.98	0.072	1.98	12.78
ANN	1.26	0.33	0.017	0.34	12.85
EMA	4.34	0.739	0.198	0.76	14.67

Table 2: Residual Analysis Girls boys ratio in Middle (VI-VIII) enrolled in India 1950 to 2005-06

The following table shows the database of ratio of Girls per 100 boys enrolled in Secondary (IX-X) in India 1950 to 2005-06

Data	Linear	Single exp	Log	Double exp	SMA	ANN	EMA
23	37.289	23.99	37.31	0	0	0	0
35	39.368	23.396	39.41	35	0	0	23
44	41.447	30.358	41.55	55.46	40.8	45.99754	33.8
50	43.526	38.543	43.73	65.4656	46.4	52.16885	42.98
52	45.605	45.417	45.93	65.7482	53.4	53.3406	49.298
51	47.684	49.366	48.14	59.95191	53.4	53.01302	51.729
57	49.763	50.346	50.36	60.17069	54.8	63.43462	51.072
57	51.842	54.338	52.58	59.11676	56	48.65185	56.407
57	53.921	55.935	54.79	57.93315	57.4	55.53744	56.94
58	56	56.574	56.98	58.08377	58.4	55.53744	56.994
58	58.078	57.429	59.15	58.11386	59.8	54.10205	57.899
62	60.157	57.771	61.28	61.9249	61	57.60895	57.989
64	62.236	60.308	63.37	65.39635	62.4	61.35775	61.598
63	64.315	62.523	65.4	65.32225	64.8	72.36003	63.759
65	66.394	62.809	67.39	66.37659	66.4	77.7963	63.075
70	68.473	64.123	69.31	71.10276	67.8	75.21649	64.807
70	70.552	67.649	71.17	72.59623	69.8	63.38566	69.48
71	72.631	69.059	72.96	73.21897	0	79.13857	69.948
73	74.71	71.664	74.67	74.58924	0	72.65847	70.894

Table 3: Result of Girls boys' ratio in Secondary (IX-X) Enrolled in India 1950 to 2005-06

Figure3 graphically shows the comparison result of Girls enrollment per 100 boys in Secondary database.

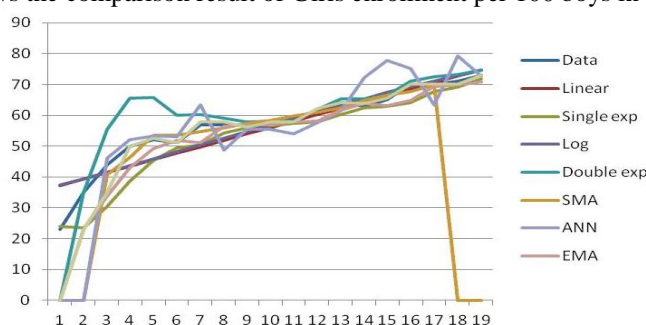


Fig 3: Comparison result of different prediction method on girls boys ratio in Secondary database

The following table shows the result of residual analysis of different prediction technique on girls boys ratio enrolled in India at Secondary (IX-X) 1950 to 2005-06.

Prediction Technique	Mean of Absolute Residual	Maximum Residual	Mean of Mean of Absolute Residual	Median Absolute Residual	Standard Deviation
Linear	15	1.55	0.082	1	11.69
Logarithm	4.1	0.877	0.58	1.88	3.5
Single exp	14.81	1.98	0.104	0.5	13.12
Double exp	13.67	1.78	0.095	1.68	13.45
SMA	16.8	2.06	0.129	2.56	12.05
ANN	1.59	0.41	0.021	0.26	12.73
EMA	5.78	0.93	0.0231	0.013	4.73

Table 4: Residual Analysis Girls boys ratio in Secondary (IX-X) enrolled in India 1950 to 2005-06

Table 5 shows the minimum error count of two different time series data in residual analysis.

Data Set	linear	Single Exp	Log	Double Exp	SMA	ANN	EMA
Girls enrollment per 100 boys (Middle)	1	0	0	0	0	4	0
Girls enrollment per 100 boys (Secondary)	0	0	1	0	0	3	1

Table 5: Minimum Error count of two different time series data in residual Analysis

IV. CONCLUSION

Here in these paper different statistical methods, smoothing methods, Artificial Neural network is applied on two different time series datasets and on the basis of residual analysis we can conclude on the fact that ANN's performance is best among other methods that has been used here.

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